

Assuming the Generalized Riemann Hypothesis and the Generalized Ramanujan Conjecture we prove sharp bounds, up to order, for products of automorphic L-functions. As corollaries we obtain large deviation estimates, as well as sharp moment bounds, up to order, for Hurwitz zeta functions with rational parameter. In this talk I will present these results and survey the methods used to prove them.