

Instead of ordering by discriminant, one may list all real quadratic fields as $F_n = \mathbb{Q}(\sqrt{n^2 - 4})$, with sparse repetitions. This family contains unit-generated orders $\mathcal{O}_n = \mathbb{Z}[\frac{1}{2}(n + \sqrt{n^2 - 4})]$; indeed, the unit-generated orders in real quadratic fields fit into two natural families, one of which is the \mathcal{O}_n . We prove that the class numbers of the orders \mathcal{O}_n grow like class numbers of imaginary quadratic fields; the other family behaves similarly. The ordering of quadratic fields F_n has several other nice features, such as a straightforward description of those with a unit of negative norm and a straightforward description of those with a unit of odd trace. In density, exactly 50% of the F_n have a unit of odd trace; in contrast, in the standard ordering by discriminant, between 7.4% and 33.4% of real quadratic fields have a unit of odd trace.

In the second part of the talk, we describe a framework of conjectures under which the class numbers of \mathcal{O}_n and its superorders count isometry classes of maximal configurations of complex equiangular lines in dimension $d = n + 1$. These configurations are known in quantum information theory as SICs (short for SIC-POVMs, or symmetric, informationally complete, positive operator-valued measures) and can be generalized to subspace configurations called r -SICs. Under our framework of conjectures, certain invariants of r -SICs are algebraic numbers that, for n odd, generate all abelian Galois extensions of F_n .

The results presented in this talk include joint work with Jeffrey Lagarias and joint work with Marcus Appleby and Steven Flammia.