

Answers to Review Document for Exam 3, Fall 2012

- 1) Vertical asymptotes: $x = 2$ and $x = 3$
Horizontal asymptote: $y = 0$ (x -axis)
- 2) Vertical asymptotes: $x = -2$, $x = 5$
Horizontal asymptote: $y = \frac{3}{2}$
- 3) Vertical asymptote: $x = \frac{1}{5}$
No horizontal asymptote
- 4) $x = -4$
- 5) $x = -11$
- 6) $x = 0$, $x = \frac{1}{2}$
- 7) \$7145.51
- 8) approximately 5.6 years
- 9) $\log_4 2 = 0.5$
- 10) $\ln 35.6 \approx 3.5723$ $e^{2.3} \approx 9.9742$
- 11) $\log_3 17 \approx 2.5789$
- 12) $x = 35$
- 13) $x = 0$ only
- 14) $c \approx 2.5932$
- 15) $\log_b 20 = 2x + y$
- 16) $\log_4 64 = 3$, $\log_3 \frac{1}{9} = -2$
- 17) $2 + \log_4 p - \frac{1}{2} \log_4 q$
- 18) (a) $-\frac{3}{5}$ (b) 0
- 19) $y' = -28e^{2x}$
- 20) $f'(x) = 2xe^{-3x}(3x - 2)$

$$21) \quad y' = \frac{1 - \ln(2x + 6)}{(x + 3)^2}$$

$$22) \quad y' = 3(x^3 + e^{2x})^2(3x^2 + 2e^{2x})$$

$$23) \quad f'(x) = \frac{e^x[x(x^2 + 2x + 2)(\ln x) - (x^2 + 2)]}{x(\ln x)^2}$$

24) slope of tangent line = $2e$ equation of tangent line: $y = (2e)x - e$

25 (a) increasing: $(-\infty, -2) \cup \left(\frac{2}{3}, \infty\right)$ (b) increasing: never

26) relative maximum: $f(-2) = 25$, relative minimum: $f(1) = -2$

27) relative maximum: $g(e^{1/2}) = 1$

$$28) \quad f''(x) = \frac{2(27x^4 + 2)}{x^3}$$

$$29) \quad g''(x) = \frac{80}{(4x + 3)^3}$$

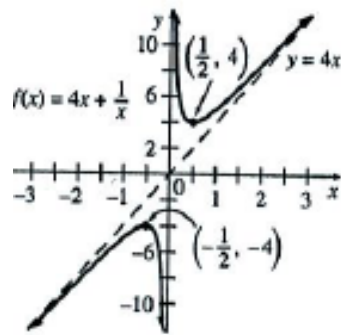
$$30) \quad f''(2) = \frac{-397}{8}, \quad f''(5) = \frac{-87494}{625}$$

31) $D = (-\infty, \infty)$, no intercepts, no horizontal asymptote, vertical asymptote: $x = 0$

Increasing: $(-\infty, -\frac{1}{2}) \cup (\frac{1}{2}, \infty)$, decreasing: $(-\frac{1}{2}, \frac{1}{2})$

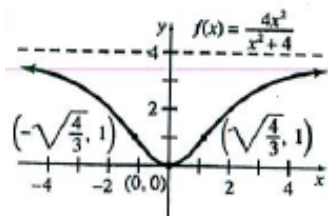
Relative maximum at point $(-\frac{1}{2}, -4)$, Relative minimum at point $(\frac{1}{2}, 4)$

Concave downward: $(-\infty, 0)$, Concave upward: $(0, \infty)$, no inflection points



Graph:

- 32) $D = (-\infty, \infty)$, intercept: $(0, 0)$ no vertical asymptote(s), horizontal asymptote: $y = 4$
 Increasing: $(0, \infty)$ Decreasing: $(-\infty, 0)$ relative minimum $(0, 0)$
 Concave upward: $(-\infty, -\sqrt{\frac{4}{3}}) \cup (\sqrt{\frac{4}{3}}, \infty)$ Concave downward: $(-\sqrt{\frac{4}{3}}, \sqrt{\frac{4}{3}})$
 Points of inflection: $(-\sqrt{\frac{4}{3}}, 1)$ and $(\sqrt{\frac{4}{3}}, 1)$



Graph: