

NOT VERY HELPFUL (SORRY) 🙄



Eigenvector dimension: nullspace

$$\dim(\text{col}) = \text{Rank}$$

$$\dim(\text{row}) = \text{Rank}$$

Defective

Defective: repeated and too many pivots in reduced form

Missing vectors: # pivots

Basis: nullspace

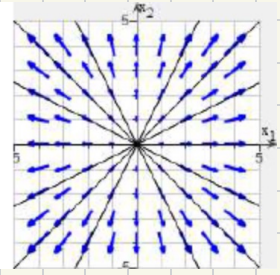
Nodal's

(repetition, state of being, sign)

Proper Nodal Source

Eigenvalues: repeated, real, positive (rrp)

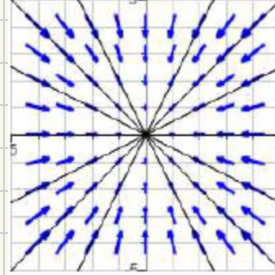
Eigenvectors: two linearly independent



Proper Nodal Sink

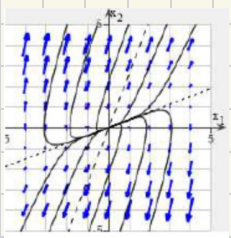
Eigenvalues: repeated, real, negative (rrn)

Eigenvectors: two linearly independent

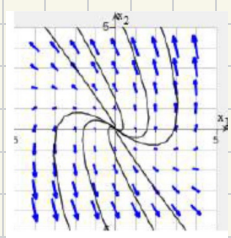


Improper Nodal Source

Eigenvector: without two linearly indp.



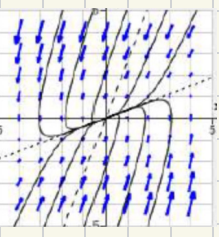
Eigenvalue: Distinct, real, positive (drp)



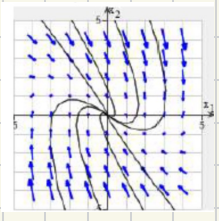
Eigenvalue: repeated, real, positive (rrp)

Improper Nodal Sink

Eigenvectors: without two linearly ind.



Eigenvalue: Distinct, real, negative (drn)

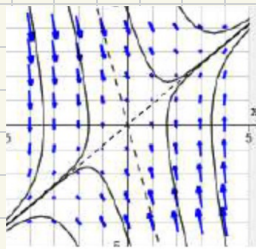


Eigenvalue: Repeated, real, negative (rrn)

Eigenvalue Dependent

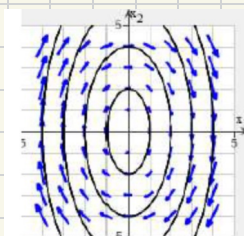
Saddle point

Eigenvalues: real, opposite sign, (not same magnitude)



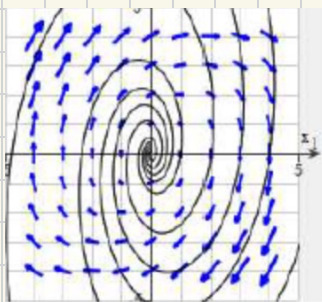
Center

Eigenvalues: imaginary



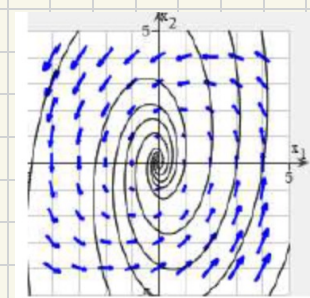
Spiral Source

Eigenvalues: Complex conjugate, real, positive



Spiral Sink

Eigenvalues: Complex conjugate, real, negative



Rules [Commonality:

Proper: two lin. ind. Eigenvectors, distinct Eigenvalues

Improper: Without two lin. ind. Eigenvectors, not distinct Eigenvalues

Source: P (positive Eigenvalue)

Sink: N (negative Eigenvalue)

Review

Bernoulli

$$V = y^{1-n} \quad V' + (1-n)P(x)V = (1-n)Q(x)$$

• Leave in terms of V' and V when solving

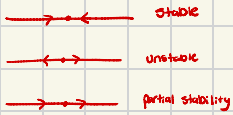
Homogeneous

$$V = \frac{y}{x} \quad y' = V + V'x$$

Stability

• Set equal to zero, solve for x

Create # line test



Application

• Newton's Law of Cooling: $\frac{dT}{dt} = K(T - S)$

Temp of object ↑
Some constant ↓
Temp of surrounding ↓

• Tank: $\frac{dy}{dt} = (\text{concentration in}) (\text{flow rate in}) - (\text{conc. out}) (\text{flow out})$

↳ $\frac{y}{\text{Volume} + (\text{min} - \text{conc out})}$

$$= \left(\frac{1}{2} \frac{\text{lb}}{\text{gal}}\right) (4 \text{ gal/min}) - \left(\frac{y}{600} \frac{\text{lb}}{\text{gal}}\right) (4 \text{ gal/min})$$

Set in tank
Value of water in tank

$$\frac{dy}{dt} = 2 - \left(\frac{y}{150}\right) (6)$$

↳ 4 in, 6 out, net loss of 2
↳ 600 - 2t (in - out)

• Spring:

Variation of parameters

$$u_1' y_1 + u_2' y_2 = 0$$

$$u_1' y_1 + u_2' y_2 = \text{right side of given equation}$$