Kiril Datchev MA 546 Spring 2025

## Homework 10

Due April 2nd on paper at the beginning of class. Please let me know if you have a question or find a mistake.

- Exercises 1 and 2 from https://www.math.purdue.edu/~kdatchev/546/sturmliouville. pdf.
- 3. Let  $\mathcal{H}$  be a Hilbert space, A a compact self-adjoint operator on  $\mathcal{H}$ , B a bounded self-adjoint operator that commutes with A. Let  $\mathcal{H}'$  be the orthogonal complement of the kernel of A. Prove that  $\mathcal{H}'$  has an orthonormal basis that is at most countable and that consists of eigenvectors of both A and B.