

- ① Let $E \subset M$ be arbitrary. Show $E \cup \partial E$ is closed; and if $F \supset E$ is closed, then $F \supset E \cup \partial E$.
(So: $E \cup \partial E$ is the smallest closed set that contains E . It is called the closure of E , denoted \bar{E} .)
- ② Show that $f: M \rightarrow P$ is continuous, $Z \subset M$ is closed does not imply $f(Z) \subset P$ is closed. (The solution should involve giving an example. Hint: Let $M = \mathbb{R}^2$, $P = \mathbb{R}$, $f(x,y) = x$. But $Z = ?$)
- ③ Give an example of a continuous map $g: M \rightarrow P$ and a compact $K \subset P$ s.t. $g^{-1}K$ is not compact.