

Today : Review for Midterm #1.

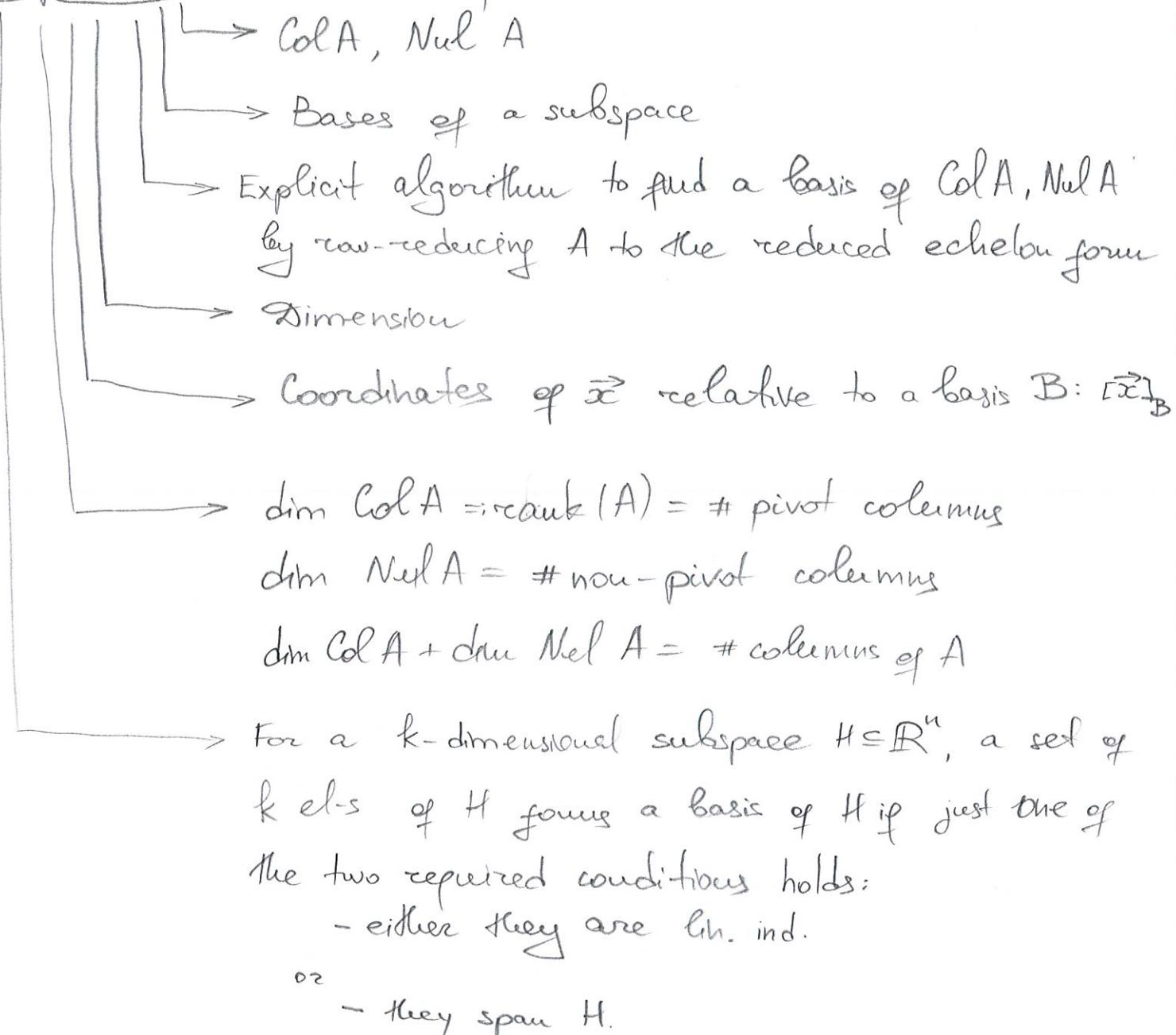
- Linear systems → Know: coefficient matrix, augmented matrix
  - Row reduction (3 types of elementary row operations)
  - Know: what "consistent" & "inconsistent" stay for.
  - Reduction to an echelon form and to the reduced echelon form (the latter requires us to move from bottom rows to the upper ones)
  - Pivot position & pivot column.
  - Basic vs Free variables
    - ↑ correspond to pivot columns
    - correspond to non-pivot columns
  - Being able to write down general solution (in case there are infinitely many parameters)
    - via the free variables & in the vector form
- Vectors → Basic operations: addition & scalar multiplication
  - Linear combination, Span
  - The way linear system may be viewed as a vector eq-n.
  - The product of a matrix and a column-vector
  - The way linear system may be viewed as a matrix eq-n.
  - $\{A\vec{x} = \vec{b}\}$  has a solution for any  $\vec{b}$   $\Leftrightarrow$  {columns of A span  $\mathbb{R}^m$ }
  - $\Leftrightarrow$  {A has pivot position in each row}.
  - Solving homogeneous matrix/Vector eqs in the parametric form
  - Solving non-homogeneous -ii- by finding a single solution and solving the associated homogeneous one.

## Lecture #12

- Linear Independence → recall properties of sets containing:
  - 1)  $\vec{0}$
  - or  
2) having  $>m$  elements of  $\mathbb{R}^m$
- (Linear) Transformations → Know: domain, codomain, image, range
  - Matrix transformations
  - Linear transformations
  - Linear transf. = Matrix transf.
  - Recovery the standard matrix of a linear transf.
  - Know: "onto" and "one-to-one" terminology
    - columns of stand. matrix span  $\mathbb{R}^n$
    - columns of stand. matrix are lin. ind.
- Matrices → Addition & Scalar Multiplication
  - Product (and its interpretation via linear transform.)
  - Transpose of matrices
  - Inverse of square matrices
  - Properties of product, transposition, and inverse.
- Inverse Matrices → Explicit f-la for  $2 \times 2$  matrices
  - General algorithm: row reduction of  $(A; I_n)$
  - Explicit f-la via the adjugate  $\text{adj } A$
  - Long list of properties equivalent to "A- invertible"

## Lecture #12

- Subspaces → General definition



- Determinants

