

Ex1: Bob wants to buy new Tissot watches. There are two stores selling the model he likes. The price in the 1st store is 400\$ and he needs to pay 7% of State taxes. The other store has the same model for 410\$, but Bob has a 4%-off coupon, while the State taxes are the same.

Where shall he buy this model of Tissot and how much will it cost Bob?

$$1^{\text{st}} \text{ Shop: } 400\$ + 0.07 \cdot 400\$ = 1.07 \cdot 400\$ = 428\$$$

$$2^{\text{nd}} \text{ Shop: } 410\$ - 0.04 \cdot 410\$ = 0.96 \cdot 410\$ - \text{the price without taxes}$$

$$1.07 \cdot 0.96 \cdot 410\$ = \underline{\underline{421.15\$}} \leftarrow \text{the price he will pay in the 2}^{\text{nd}} \text{ store.}$$

Answer: Bob will spend less when buying in the 2nd store, where he will end up by paying 421\$ 15¢

Ex2: The inflation rate in 2015 was 2%. Use this rate to find what salary at the end of 2014 would be equivalent to a \$60,000 salary at the end of 2015.

All we need to do is to compute

$$\frac{\$60,000}{1.02} = \underline{\underline{58,823\$}}$$

$\xrightarrow{1 + \frac{2\%}{100\%}}$

Ex3 (Exercise 10.1.15) A shoe store marks up the price of its shoes at 120% over cost. A pair of shoes goes on sale for 20% off, then goes on the clearance rack for an additional 30% off. A customer walks in with a 10% off coupon and buys the shoes. Express the store's profit on these shoes as a percentage of the original cost

$$(1+1.2) \cdot (1-0.2) \cdot (1-0.3) \cdot (1-0.1) = 1+0.1088 \Rightarrow \text{profit is } \underline{\underline{10.88\%}}$$

Remk: Point out the relation b/w the growth rate from last lecture and the percentage increase / decrease in values in the current topic.

Warnings: (1) If your stock portfolio goes up 25% one day and goes down 20% next day, then you do not make 5% over these two days. Instead, you get what you started from since $(1+0.25) \cdot (1-0.2) = 1$.

(2) Sometimes stores advertise discount of $>100\%$ (see Ex 10.6). Mathematically they are wrong!

• Simple Interest

Initial data & terminology:

- Principal (P) - the sum of \$ that Lender (L) lends to Borrower (B)
- Interest rate (r) - the rate paid by B to L for using P over a particular period of time, e.g. a year.
In the case when interest rate is expressed as % of P over a year, then the rate is called APR.
- Term (t) - the length of time the B is borrowing money.
- Repayment Schedule
 - single payment: paying off the loan in a lump sum @ end
 - installment loan: repays making equal monthly payments
- Interest
 - single: the interest rate is applied only to P
 - compound: the interest accumulates

Simple Interest Formula: $I = t \cdot r \cdot P$ or Future payoff $F = P \cdot (1 + t \cdot r)$

! Ex. 10.9 on bonds.