

4. (b) RECALL: WE REDUCED THE QUESTION TO SOLVING

$$\begin{bmatrix} 0 & 2 & 1 \\ 3 & 3 & 1 \\ 1 & 5 & 3 \\ 4 & 7 & 4 \end{bmatrix} \begin{bmatrix} c_1 \\ c_2 \\ c_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

HOW,

$$\begin{bmatrix} 0 & 2 & 1 \\ 3 & 3 & 1 \\ 1 & 5 & 3 \\ 4 & 7 & 4 \end{bmatrix} \xrightarrow{\text{ERDs}} \begin{bmatrix} 1 & 5 & 3 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{aligned} \therefore c_1 + 5c_2 + 3c_3 &= 0 \\ c_2 &= 0 \\ c_3 &= 0 \end{aligned}$$



$$c_1 = c_2 = c_3 = 0 \quad (\text{BACK-SUBST.})$$

$\Rightarrow$  L.I.

$$\begin{bmatrix} 0 & 2 & 1 \\ 3 & 3 & 1 \\ 1 & 5 & 3 \\ 4 & 7 & 4 \end{bmatrix} \xrightarrow{P_{13}} \begin{bmatrix} 1 & 5 & 3 \\ 3 & 3 & 1 \\ 0 & 2 & 1 \\ 4 & 7 & 4 \end{bmatrix} \xrightarrow{\substack{A_{12}(-3) \\ A_{14}(-4)}} \begin{bmatrix} 1 & 5 & 3 \\ 0 & -12 & -8 \\ 0 & 2 & 1 \\ 0 & -13 & -8 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 5 & 3 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix} \xleftarrow{A_{34}(-8)} \begin{bmatrix} 1 & 5 & 3 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & -8 \end{bmatrix} \xleftarrow{\substack{A_{23}(-2) \\ A_{24}(13)}} \begin{bmatrix} 1 & 5 & 3 \\ 0 & 1 & 0 \\ 0 & 2 & 1 \\ 0 & -13 & -8 \end{bmatrix} \xrightarrow{A_{42}(-1)} \begin{bmatrix} 1 & 5 & 3 \\ 0 & 1 & 0 \\ 0 & 2 & 1 \\ 0 & -13 & -8 \end{bmatrix}$$

25.

WTS

$$\begin{bmatrix} 4 & 3 & 2 & -1 \\ 5 & 4 & 3 & -1 \\ -2 & -2 & -1 & 2 \\ 11 & 6 & 4 & 1 \end{bmatrix}$$

EROS

$$\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & -3 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \boxed{4} & 3 & 2 & -1 \\ 5 & 4 & 3 & -1 \\ -2 & -2 & -1 & 2 \\ 11 & 6 & 4 & 1 \end{bmatrix}$$

$A_{12}(-1)$

$$\begin{bmatrix} \boxed{4} & 3 & 2 & -1 \\ 1 & 1 & 1 & 0 \\ -2 & -2 & -1 & 2 \\ 11 & 6 & 4 & 1 \end{bmatrix}$$

$\uparrow_{12}$

$$\begin{bmatrix} \boxed{1} & 1 & 1 & 0 \\ 4 & 3 & 2 & -1 \\ -2 & -2 & -1 & 2 \\ 11 & 6 & 4 & 1 \end{bmatrix}$$



$$\begin{bmatrix} 1 & 0 & -1 & -1 \\ 0 & 0 & 2 & 1 \\ 0 & 0 & \boxed{1} & 2 \\ 0 & 0 & 3 & 6 \end{bmatrix}$$

$M_2(-1)$

$$\begin{bmatrix} 1 & 0 & -1 & -1 \\ 0 & \boxed{-1} & -2 & -1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 3 & 6 \end{bmatrix}$$

$A_{21}(1)$

$A_{24}(-5)$

$$\begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & \boxed{-1} & -2 & -1 \\ 0 & 0 & 1 & 2 \\ 0 & -5 & -7 & 1 \end{bmatrix}$$

$A_{12}(-4)$   
 $A_{13}(2)$   
 $A_{14}(-11)$

$A_{34}(-3)$   $A_{31}(1)$   
 $A_{32}(-2)$

$$\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & -3 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$