

FORMULA SHEET

Trigonometric Functions and Identities

$$\begin{aligned}\sin^2 x + \cos^2 x &= 1 & 1 + \tan^2 x &= \sec^2 x & 1 + \cot^2 x &= \csc^2 x \\ \sin(x+y) &= \sin x \cos y + \sin y \cos x & \cos(x+y) &= \cos x \cos y - \sin x \sin y\end{aligned}$$

Single-Variable Integrals (the constants are omitted)

$$\begin{array}{ll} \int x^n dx = \frac{x^{n+1}}{n+1} & (n \neq -1) \\ \int e^{ax} dx = \frac{e^{ax}}{a} & \\ \int \cos x dx = \sin x & \\ \int -\csc^2 x dx = \cot x & \\ \int \csc x \cot x dx = -\csc x & \\ \int \csc x dx = \ln |\csc x - \cot x| & \\ \int \cot x dx = \ln |\sin x| & \\ \int \frac{1}{\sqrt{a^2 - x^2}} dx = \arcsin\left(\frac{x}{a}\right) & \\ \int \frac{1}{x^2 - a^2} dx = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right| & \end{array} \quad \begin{array}{l} \int \frac{1}{x} dx = \ln |x| \\ \int \sin x dx = -\cos x \\ \int \sec^2 x dx = \tan x \\ \int \sec x \tan x dx = \sec x \\ \int \sec x dx = \ln |\sec x + \tan x| \\ \int \tan x dx = \ln |\sec x| \\ \int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \arctan\left(\frac{x}{a}\right) \\ \int \frac{1}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right| \end{array}$$