

Outline

- 1 Introduction
- 2 The basic principle of counting
- 3 Permutations
- 4 Combinations
- 5 Multinomial coefficients

A simple example of counting

Functional



Non functional



$n = 4$, $m = 2$ defective
 $n - m = 2$ non defective

A communication system:

- Setup: n antennas lined up
- Functional system:
↔ when no 2 consecutive defective antennas
- We know that m antennas are defective

Problem: compute

P (functional system)

Example: $n = 4$ $m = 2$ defective

0 \rightarrow defective

1 \rightarrow non defective

For small n, m : enumerate all possibilities

0 0 1 1

1 0 0 1

0 1 0 1

functional

1 0 1 0

0 1 1 0

1 1 0 0

$P(\text{functional}) =$

$\frac{\# \text{ functional systems}}{\# \text{ systems}}$

$$= \frac{3}{6} = \frac{1}{2}$$

For larger values of n, m

↳ need to count!

A simple example of counting (2)

Particular instance of the previous situation:

- Take $n = 4$ and $m = 2$
- Possible configurations:

0011	0101	0110
1001	1010	1100

- We get 3 working configurations among 6, and thus

$$\mathbf{P}(\text{functional system}) = \frac{1}{2}$$

Conclusion: need an effective way to count, that is

Combinatorial analysis